

$$\theta(k, \omega) = \int \frac{d^3 q}{(2\pi)^3} \left[\frac{1 - f_{q-k/2}^\uparrow - f_{q+k/2}^\downarrow}{\omega - q^2/m - k^2/4m} + \frac{m}{q^2} \right]$$