

$$\delta\Omega = -\pi \int \frac{d^3 k}{(2\pi)^3} \int \frac{d\omega}{2\pi} \frac{1}{e^{\beta\omega} - 1} \delta_k(\omega)$$