

$$\Gamma_{\downarrow}(\omega, k) = \int \frac{d^3q}{(2\pi)^3} \Lambda(\omega + \epsilon_q^{\uparrow}, k + q) [f_q^{\uparrow} + g(\omega + \epsilon_q^{\uparrow})]$$