

University of
Connecticut

Aspen Center for
PHYSICS

Workshop on
Quantum Simulation/Computation
with Cold Atoms and Molecules

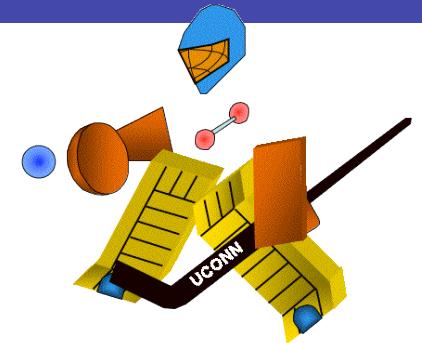
AMO Tutorial 2: cold atoms

by Robin Côté

Aspen, Wednesday June 3 2009



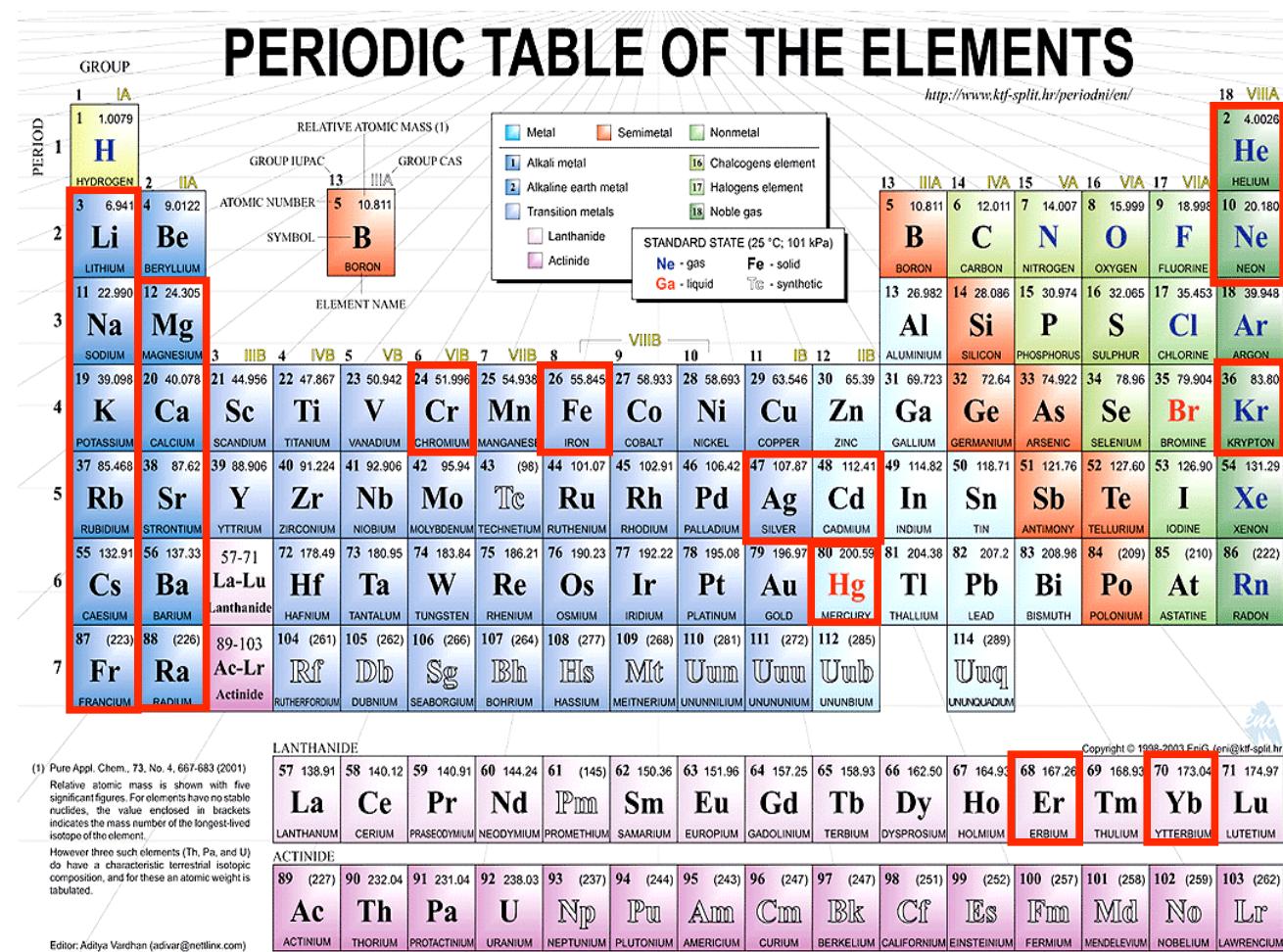
Outline



- Introduction/motivation
 - Property wish list
- Overview of AMO platforms
- Trapped ion / atom-ion systems
- **Cold atoms**
 - **Rydberg atoms**
- Cold molecules
- Other applications
- Concluding remarks

Cold Atoms

- The list is growing



-2-level cycling
transitions

-available transitions

Quantum computer wish list

- Stable trapping/storage
- Addressable qubits
- Gates between (separated) qubits
- Long coherence-, short interaction-times
- Scalability
- Strong, switchable interaction
- Readout/initialization

Collisional gate

- Phase gate
 - Each site initially in superposition of $|0\rangle$ and $|1\rangle$

$$|A\rangle \sim |0\rangle_A + |1\rangle_A$$

$$|B\rangle \sim |0\rangle_B + |1\rangle_B$$

$$|Q\rangle \sim |00\rangle + |01\rangle + |10\rangle + |11\rangle$$

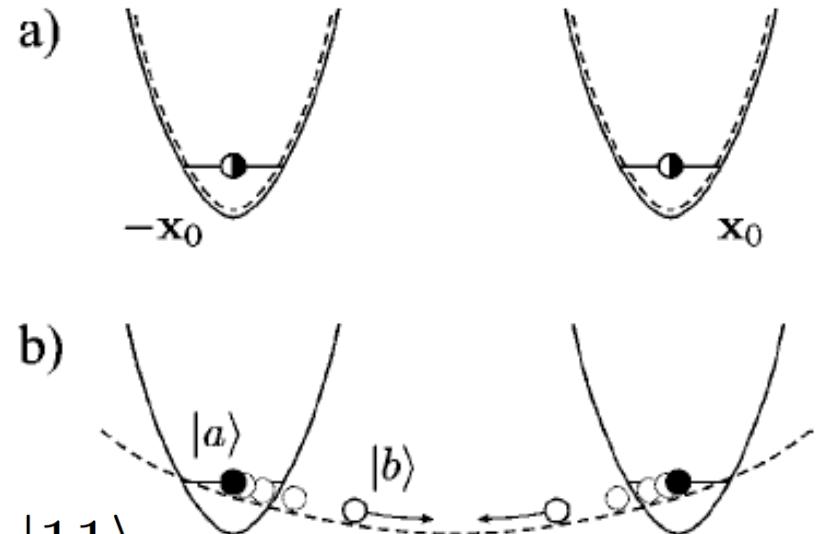
- Change the trap for state $|1\rangle$

- Collision induce a phase

$$|Q\rangle \sim |00\rangle + |01\rangle + |10\rangle + e^{i\phi}|11\rangle$$

- $\phi = \pi$: phase gate

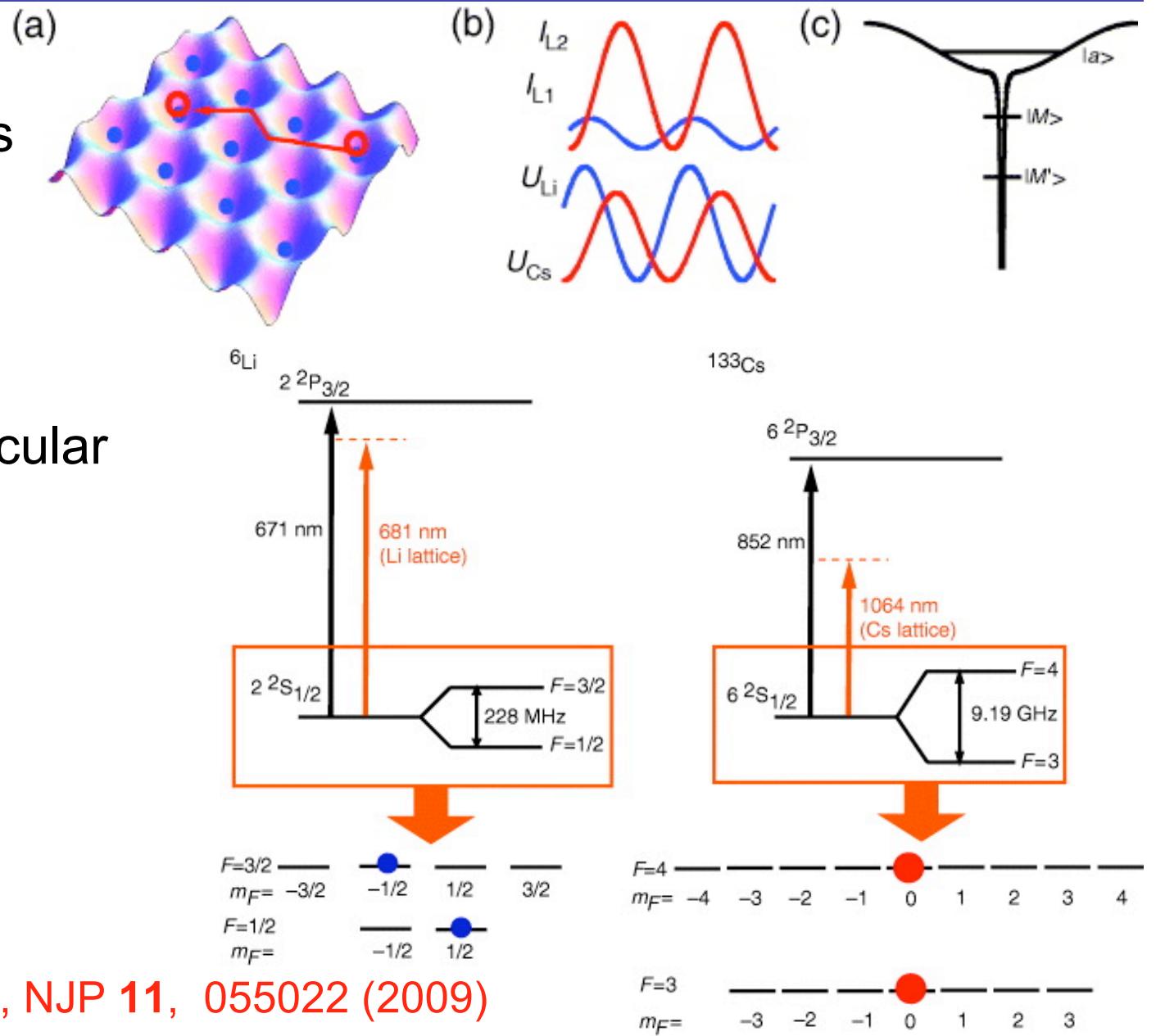
$$|Q\rangle \sim |00\rangle + |01\rangle + |10\rangle - |11\rangle$$



Cirac-Zoller, PRA 61, 022304 (2000)

Using a mixture

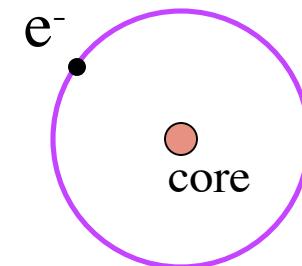
- C. Chin
 - ${}^6\text{Li}$ and ${}^{133}\text{Cs}$
- Not exactly collisional
 - Needs molecular states



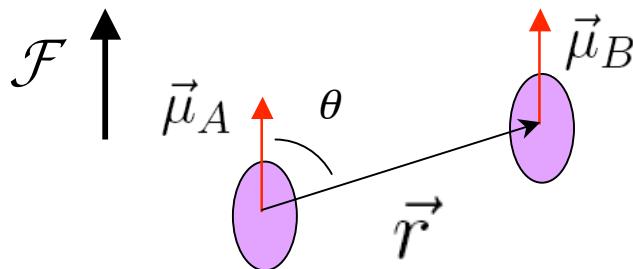
C. Chin & co-workers, NJP 11, 055022 (2009)

Rydberg Atoms

- Alkali atoms are good candidates to encode qubits:
 - Measurement high quantum efficiency: e.g., cycling transition.
 - Easy cooling and trapping
 - Low decoherence times.
- Rydberg atoms resemble hydrogen atom:
 - Radius and dipole moment scale as n^2
 - Energy $\propto 1/(n-\delta_{n,\ell})^2$, quantum defect $\delta_{n,\ell}$
- Long lifetimes $\propto n^3$. $50p$, $\tau=238 \mu\text{s}$ ($\tau=.02 \mu\text{s}$ for $5p$)
- Large polarizability $\propto n^7$: Stark mixing other ℓ by electric fields \mathcal{F}



$$|49p\rangle = \alpha |49p\rangle + \beta |49s\rangle + \dots \text{ with } \beta = 0.11 \mathcal{F} \Rightarrow \tilde{\mu}_{pp} = 2\alpha \beta \mu_{sp}$$



$$V_{d-d} = \frac{\vec{\mu}_A \cdot \vec{\mu}_B}{r^3} - 3 \frac{(\vec{r} \cdot \vec{\mu}_A)(\vec{r} \cdot \vec{\mu}_B)}{r^5}$$

Long-range wells

- Higher dispersion terms

- $np+ns$ or $np+nd$:

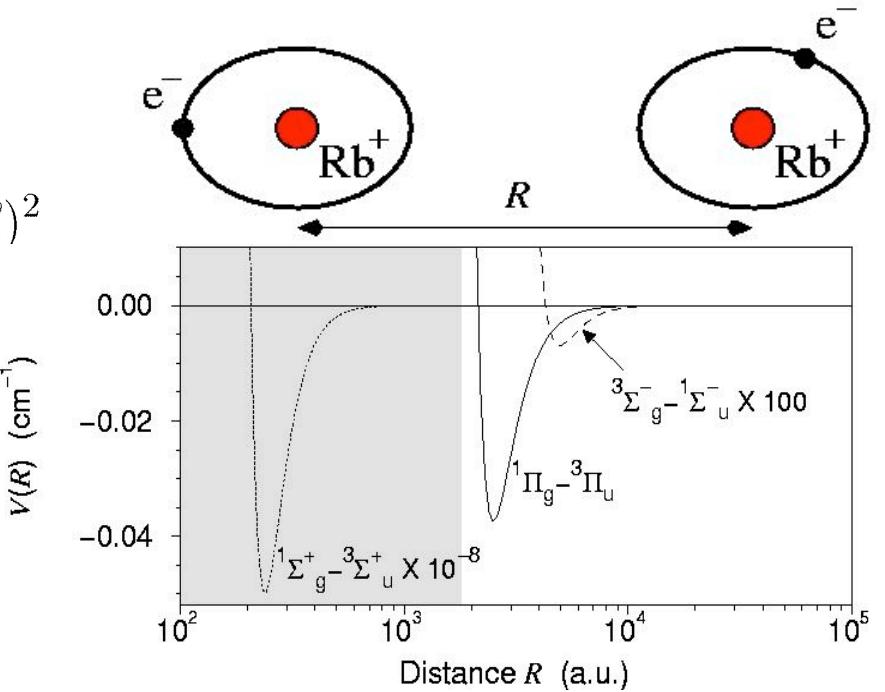
$$V(R) = \frac{C_3}{R^3} \text{ with } C_3 = A(np|r|n\ell)^2$$

- $np+np$:

$$V(R) = -\frac{C_5}{R^5} - \frac{C_6}{R^6} - \frac{C_8}{R^8}$$

$$C_3 \propto n^4, C_5 \propto n^8$$

$$C_6 \propto n^{11}, C_8 \propto n^{15}$$



- Combination of coefficients can lead to long-range wells
 - “stable” if electron wave functions do not overlap (non-shaded region)
 - very extended molecules (few μm or more) : macrodimers
 - shallow wells can exist only in ultracold regime
- $n=70$: $D_e \sim 300$ kHz and $R_e \sim 100,000$ a_0 (100 levels spaced by a few kHz)

C. Boisseau, I. Simbotin, & R. Côté, PRL 88, 133004 (2002)

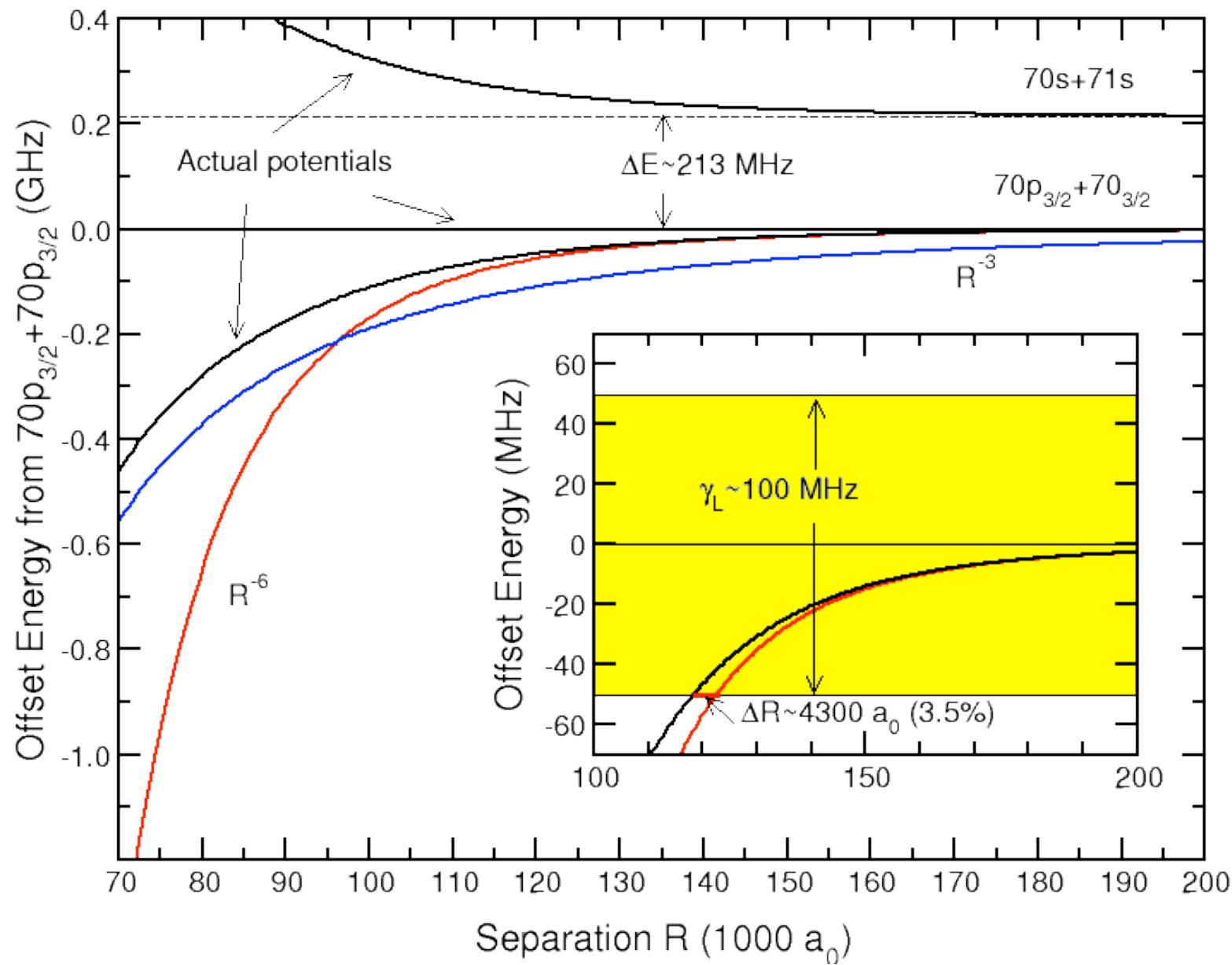
Mixed states

- When $\left| \frac{C_6}{R^6} \right| \sim \Delta E$, need to include couplings between states splitted by ΔE at $R \rightarrow \infty$
- Simple treatment with $np+np$ and $ns+n's$ asymptotes
 - E.g., atomic states for $70p+70p$ and $70s+71s$ mix
 - Asymptotic form of electronic wave functions of atom pairs $|pp(1)\rangle$, $|pp(2)\rangle$ and $|ss'\rangle$ contain dipole-dipole terms
 - Need to diagonalize interactions (with correct symmetries and dipole moments)

$$\begin{pmatrix} 0 & 0 & AR^{-3} \\ 0 & 0 & BR^{-3} \\ AR^{-3} & BR^{-3} & \Delta E \end{pmatrix}$$

$$A = \frac{2}{3} \mu_{ps} \mu_{ps'}$$
$$B = \frac{4}{3\sqrt{2}} \mu_{ps} \mu_{ps'}$$
$$\Delta E \sim 213 \text{ MHz}$$

Coupled potential curves



Application: Phase Gate

- “Simple” phase control gate
 - use atoms in an optical lattice
 - state prepared by Raman pulses

$$|A\rangle = \frac{1}{\sqrt{2}} \{ |0\rangle + |1\rangle \}$$

$$|B\rangle = \frac{1}{\sqrt{2}} \{ |0\rangle + |1\rangle \}$$

- Two-qubit state

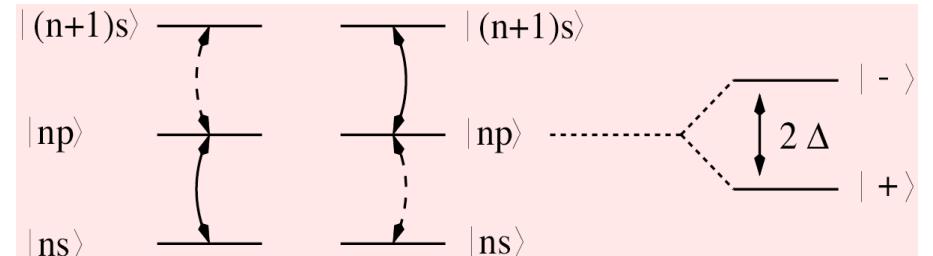
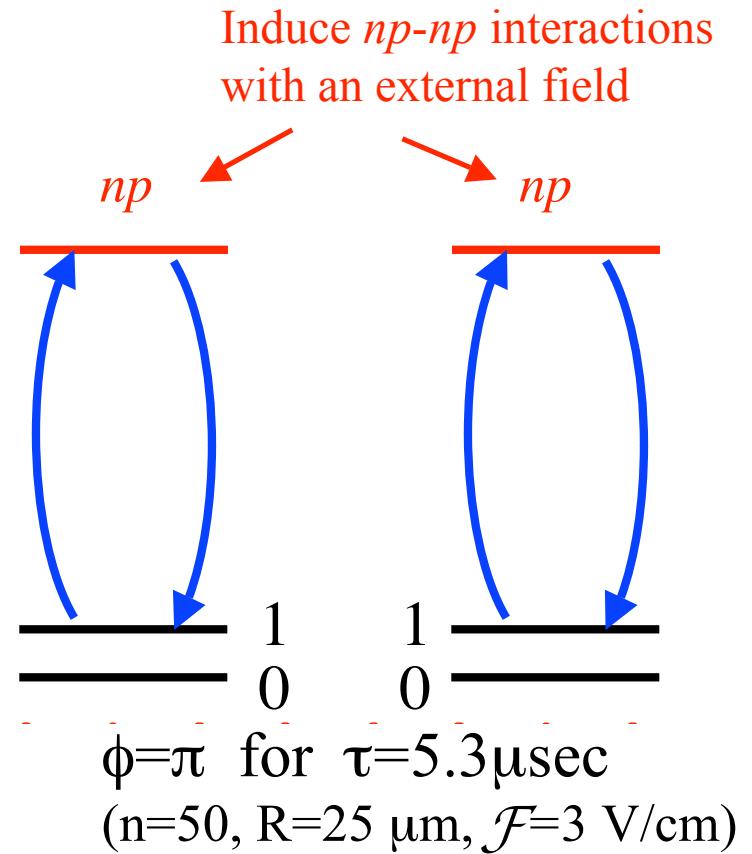
$$|Q\rangle \neq |A\rangle \otimes |B\rangle$$

$$|Q\rangle = |00\rangle + |01\rangle + |10\rangle - |11\rangle$$

- Possible also with excitation blockade

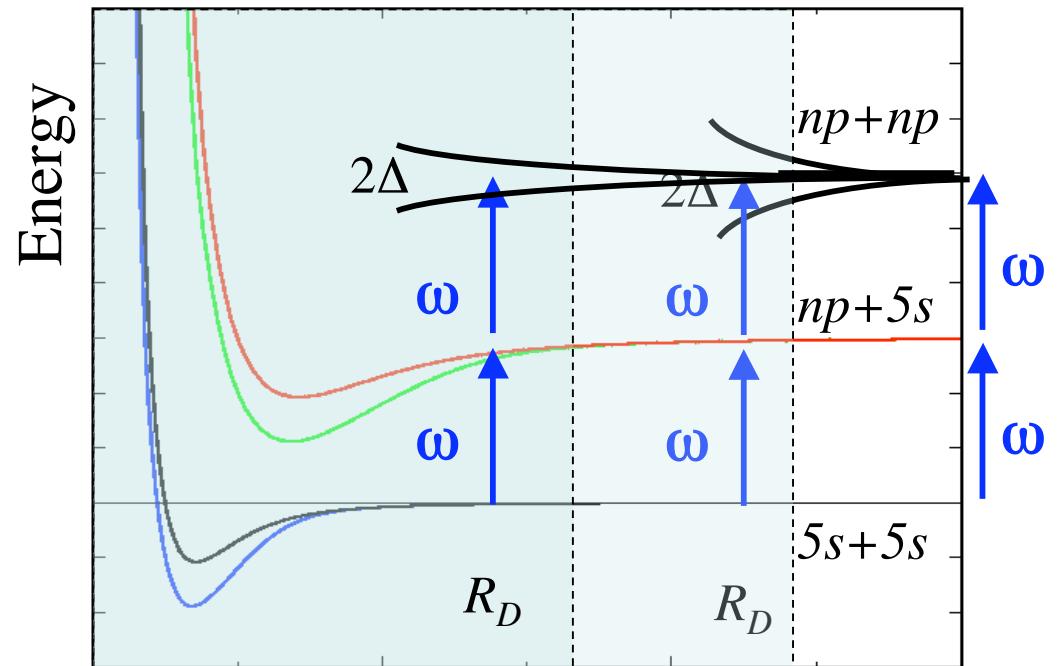
- strong dipole-dipole interactions
- degenerate states split
- laser pulse sequence gives a phase gate

D. Jaksch *et al.*, PRL 85, 2208 (2000).



Application: Excitation Blockade

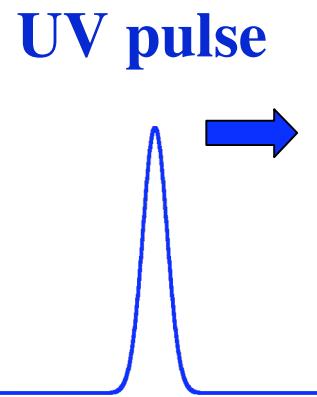
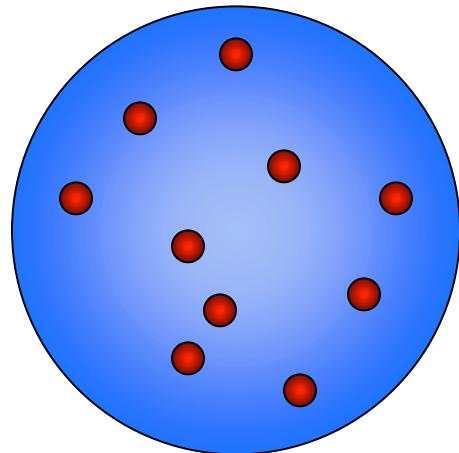
- van der Waals $\propto n^{11}$
 - interactions shift the two-photon resonance
- Low n or densities
 - Weak interactions between Rydberg atoms
 - 2-photon resonance is shifted at “small” R
 - below R_D , excitation of 2 Rydberg atoms (or more) is prohibited
 - Isolated atom behavior



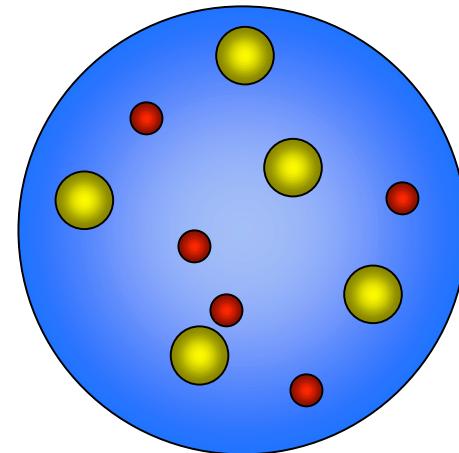
- Separation R
- large n or densities
 - strong molecular interactions
 - resonance shifted at large R
 - *Blockaded* behavior

A sketch

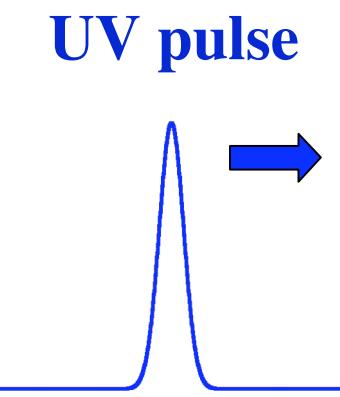
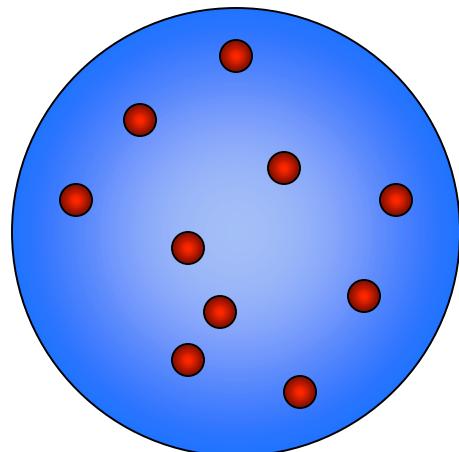
Isolated atom behavior



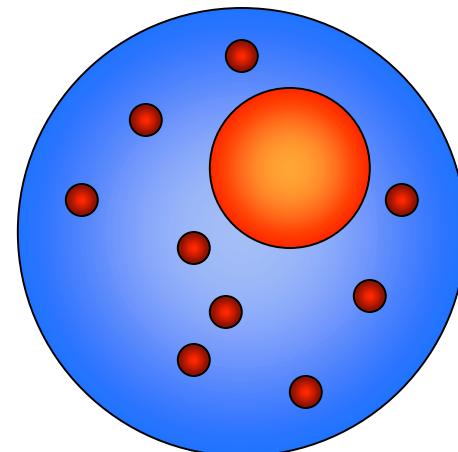
Weak interactions/low n



Blockaded atom behavior



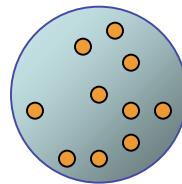
Strong interactions/high n



Blockade & gates

- Ensemble of atoms

- few μm in size
- 10-100 atoms



- Collective states

$|g\rangle$: All atoms in ground state.

$|q^n\rangle$: Collective state of n-atoms in q .

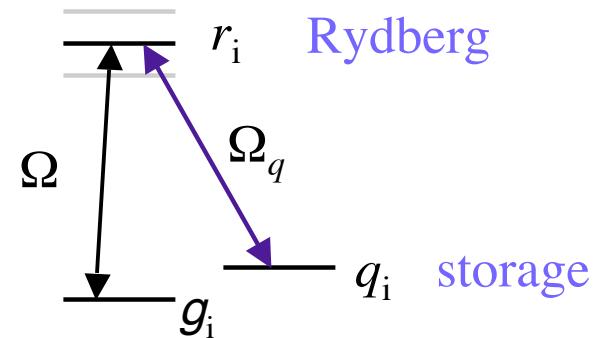
$|r^1\rangle$: Only one excitation allowed in r .

- Prepare initial state

$$|g\rangle \xrightarrow{\Omega\sqrt{N}} |r^1\rangle \xrightarrow{\Omega_q} |q^1\rangle$$

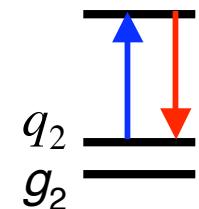
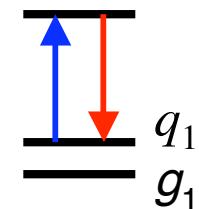
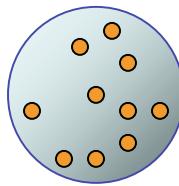
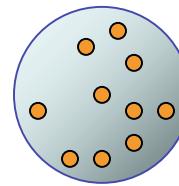
- Based on conditional excitation
- Ensemble behaves as a “super-atom”

- Single-atom levels:



- Phase gate

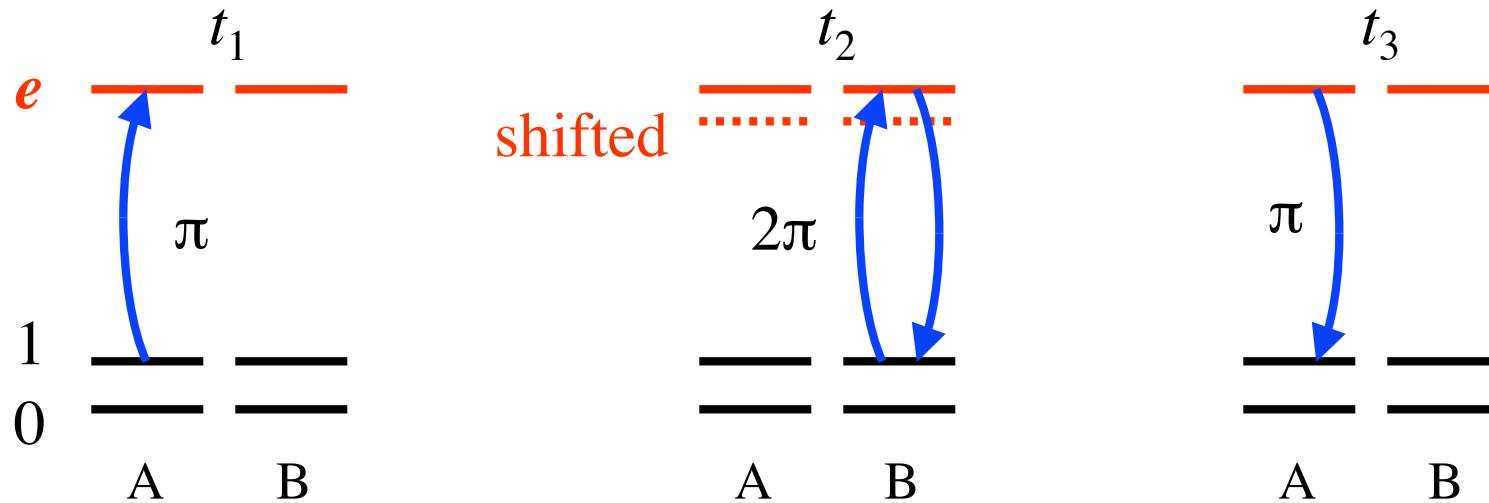
$$\begin{array}{ll} |g_1g_2\rangle \rightarrow |g_1g_2\rangle & |g_1q_2\rangle \rightarrow |g_1q_2\rangle \\ |q_1g_2\rangle \rightarrow |q_1g_2\rangle & |q_1q_2\rangle \rightarrow -|q_1q_2\rangle \end{array}$$



M.D. Lukin, M. Fleischhauer, R. Côté, L.M. Duan, D. Jaksch, J.I. Cirac, and P. Zoller, PRL 87, 037901 (2001)

Gate using Blockade

- If sites individually addressable and shift large



$$|Q_0\rangle = |00\rangle + |01\rangle + |10\rangle + |11\rangle$$

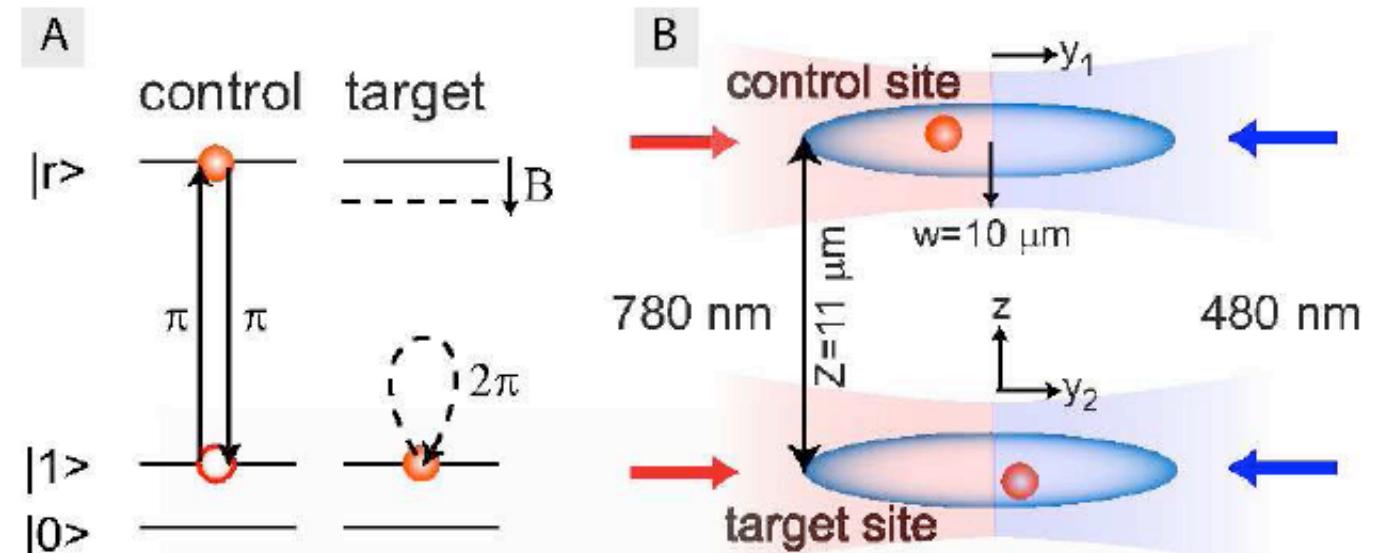
$$|Q_1\rangle = |00\rangle + |01\rangle + i|\textcolor{red}{e}0\rangle + i|\textcolor{red}{e}1\rangle$$

$$|Q_2\rangle = |00\rangle + i^2|01\rangle + i|\textcolor{red}{e}0\rangle + \boxed{i|\textcolor{red}{e}1\rangle} \quad \leftarrow \text{blockaded}$$

$$\begin{aligned} |Q_3\rangle &= |00\rangle + i^2|01\rangle + i^2|10\rangle + i^2|11\rangle \\ &= |00\rangle - |01\rangle - |10\rangle - |11\rangle \end{aligned}$$

D. Jaksch *et al.*, PRL 85, 2208 (2000).

Observation with 2 atoms

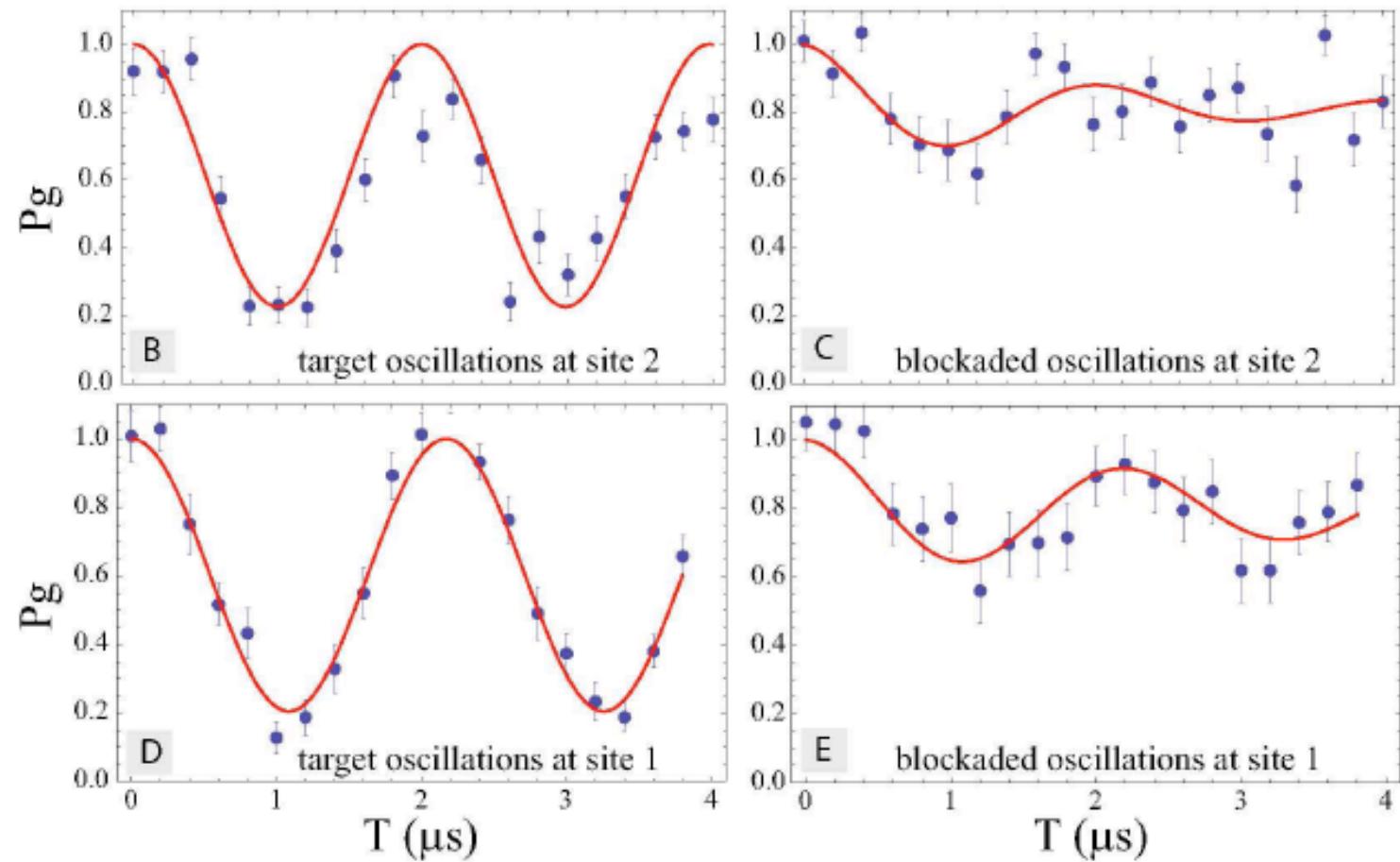


- Target excitation depends on state of control

E. Urban et al., Nature Phys. (2009).

Results

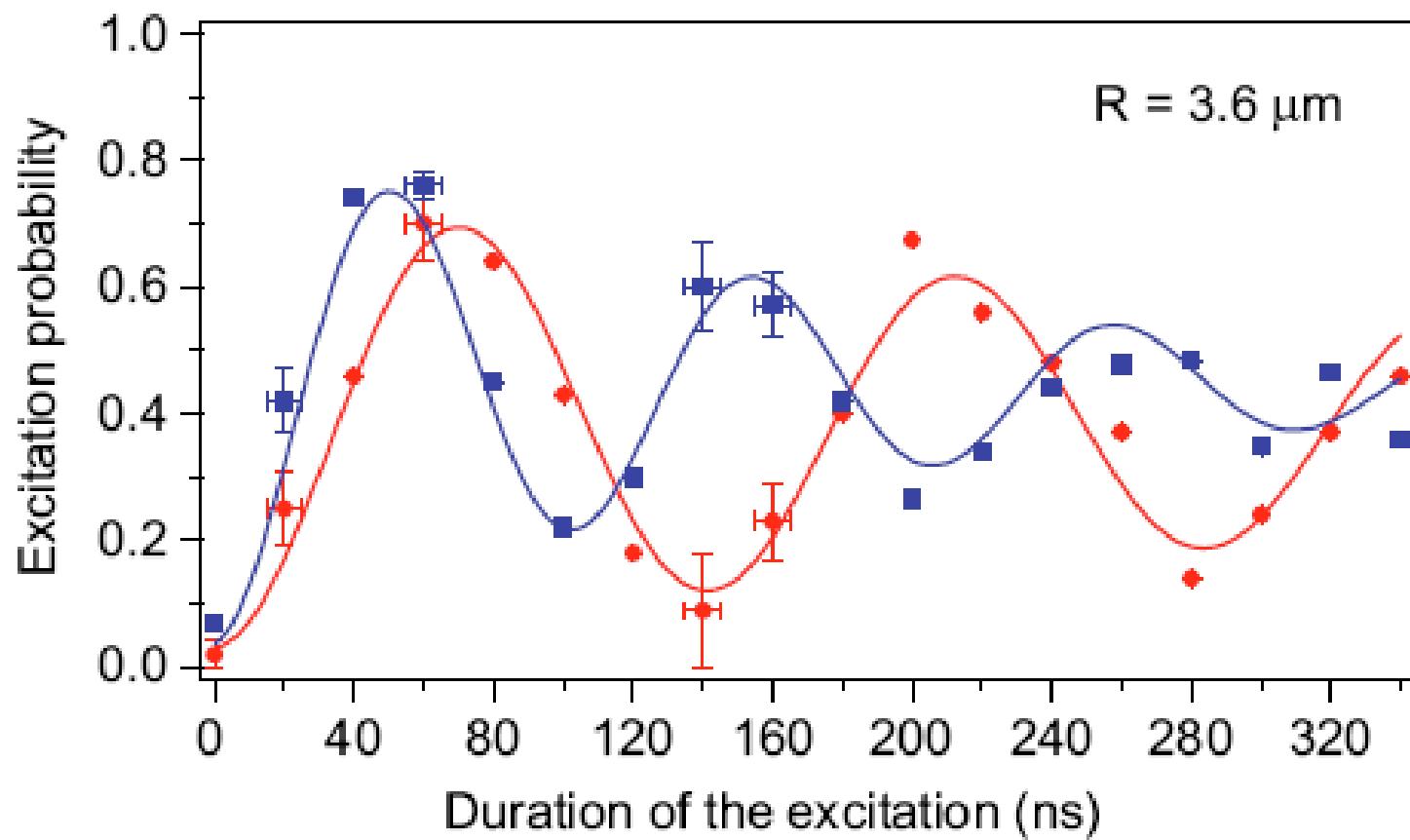
- If control is excited ($n=79$)
 - Lower probability of exciting the target



E. Urban et al., Nature Phys. (2009).

Many-body excitation

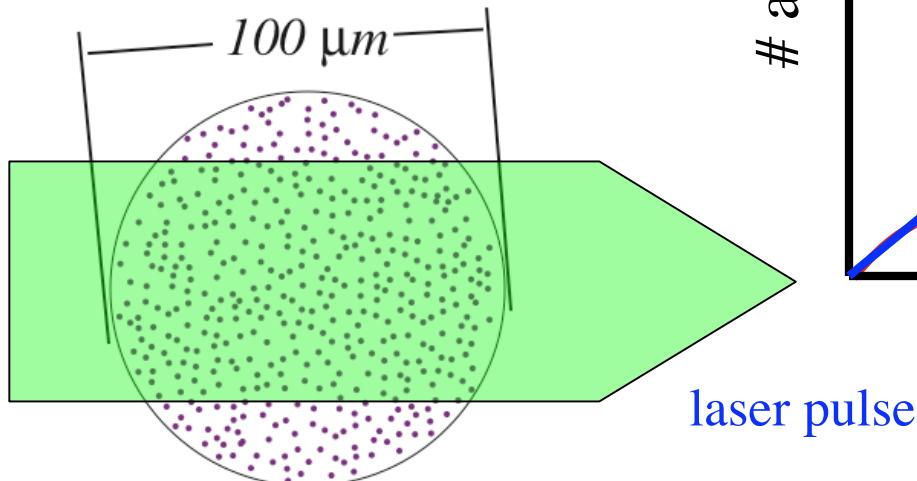
- When 2 atoms are excited in $58d_{3/2}$
 - Rabi frequency is $\sqrt{2} \Omega$



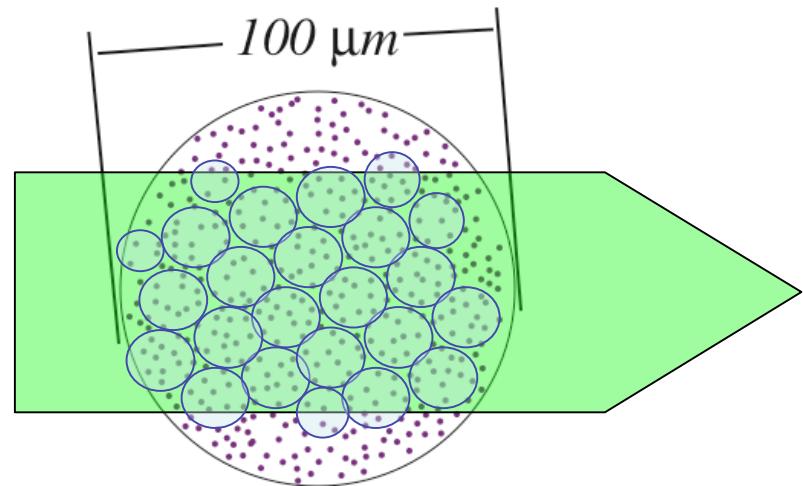
A. Gaëtan et al., Nature Phys. (2009).

About a larger sample ?

- low n or densities
 - isolated atom behavior

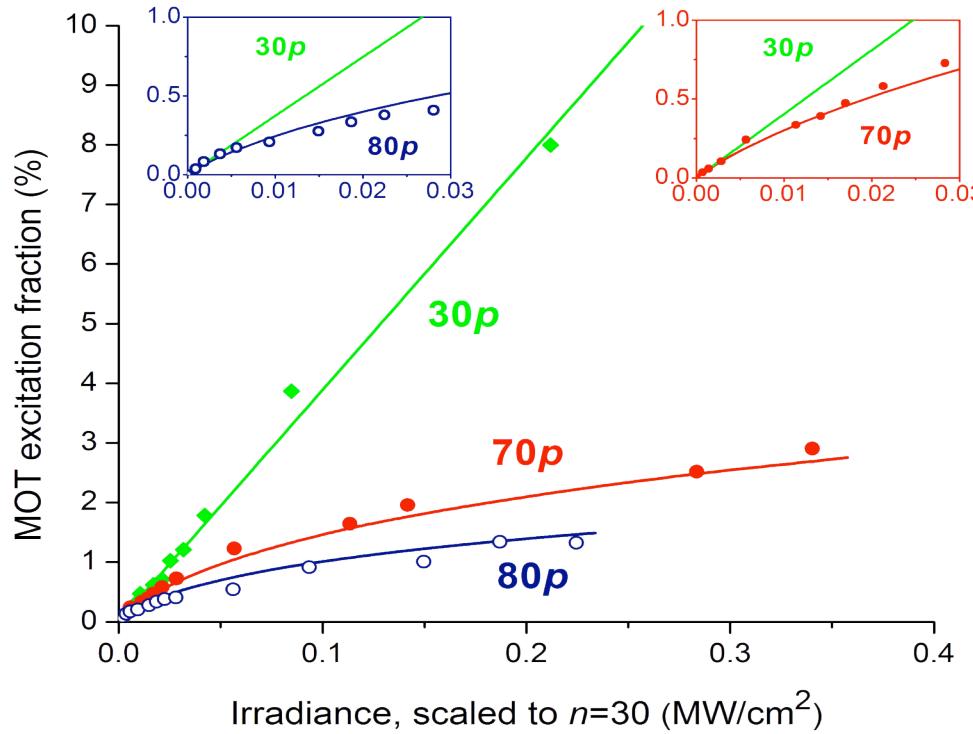


- large n or densities
 - locally blockaded domains



Measurements

- Excitation blockade:

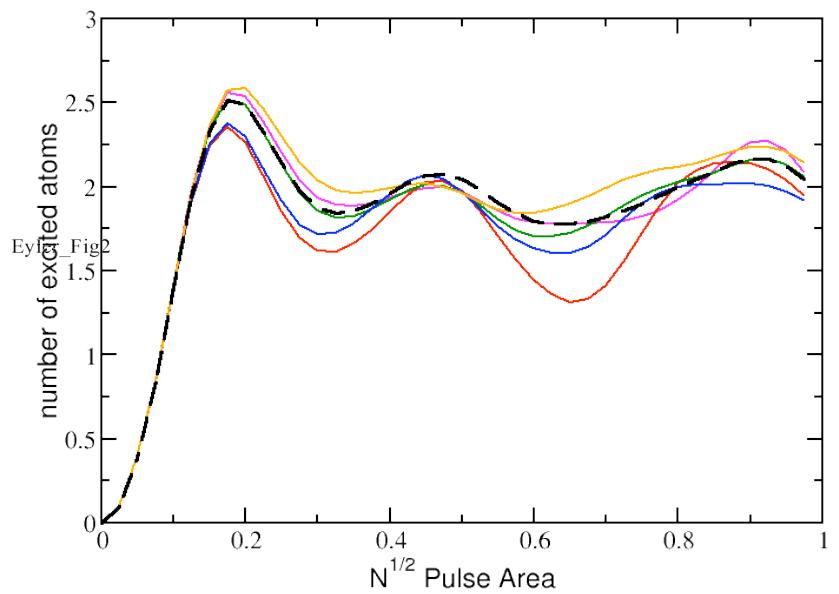


D. Tong *et al.*, PRL **93**, 063001 (2004).

K. Singer, *et al.*, PRL **93**, 163001 (2004).

- Many-body oscillation

- difficult in large sample
- Pfau in Rb BEC
- $n=90, 70$ atoms, 10^{11} cm^3 , $\tau = 10$ ns

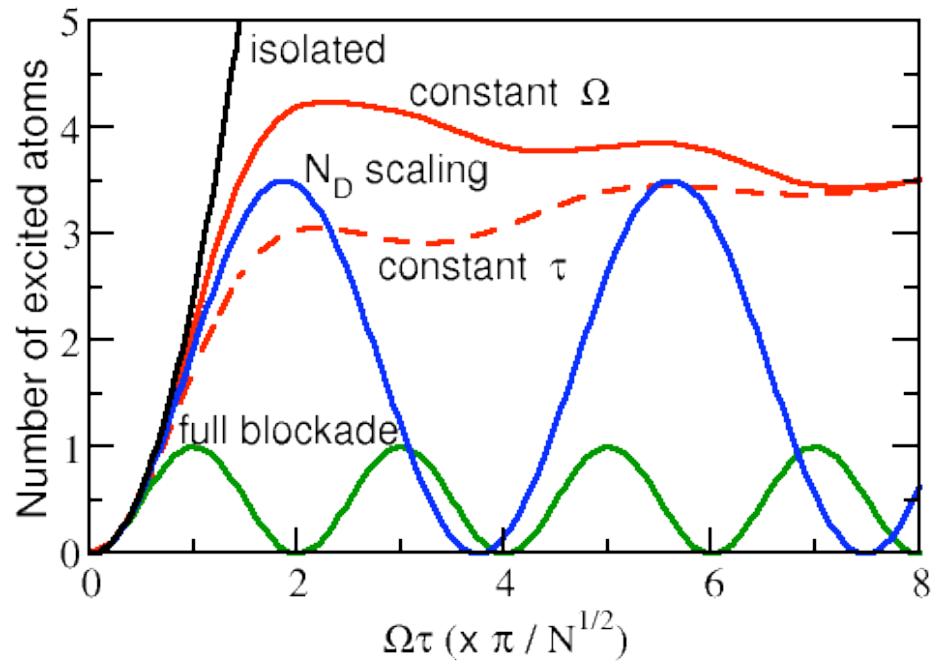
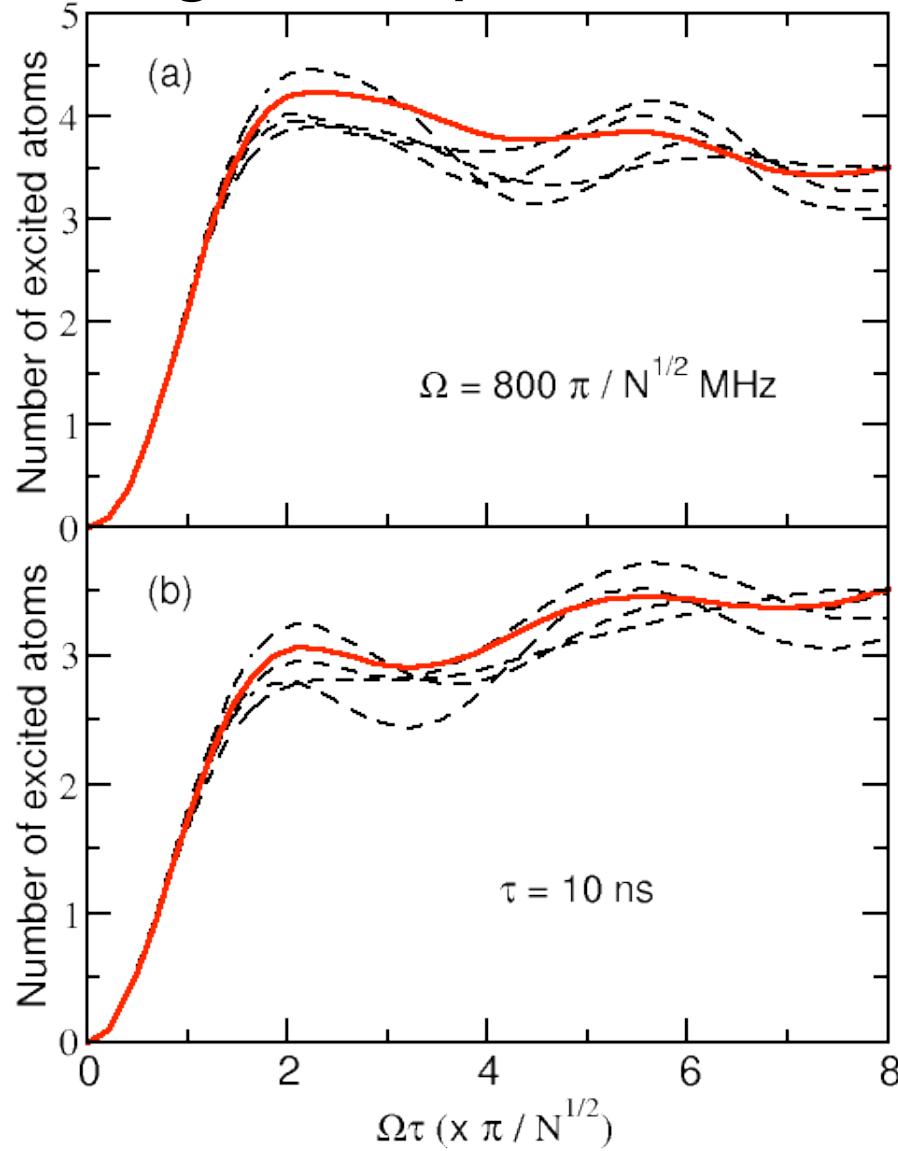


- Dipole blockade

- observed by Pillet

Results from simulations

- Large sample: 70 atoms and up to 7 excitations



- 70p atoms
 - Rabi frequency scales
 $\sqrt{N_D} \Omega$

Many-body treatment

- Hamiltonian with 2-level atom i

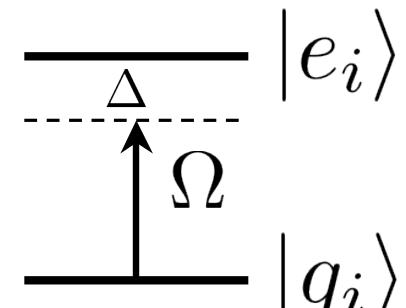
$$H = \Delta \sum_{i=1}^N \hat{\sigma}_{ee}^i - \frac{\Omega}{2} \sum_{i=1}^N (f(t) \hat{\sigma}_{eg}^i + f^*(t) \hat{\sigma}_{ge}^i) + \sum_{i \neq j > i} \kappa_{ij} \hat{\sigma}_{ee}^i \hat{\sigma}_{ee}^j$$

- With definitions

$$\hat{\sigma}_{eg}^i \equiv |e_i\rangle\langle g_i|$$

$$\kappa_{ij} = \frac{C_6}{R_{ij}^6}$$

$$f(t) = e^{-t^2/\sigma^2 - i\beta t^2}$$



Simplification

- Equation of motion for σ -operators
- Removing the Δ term using new scaled variables

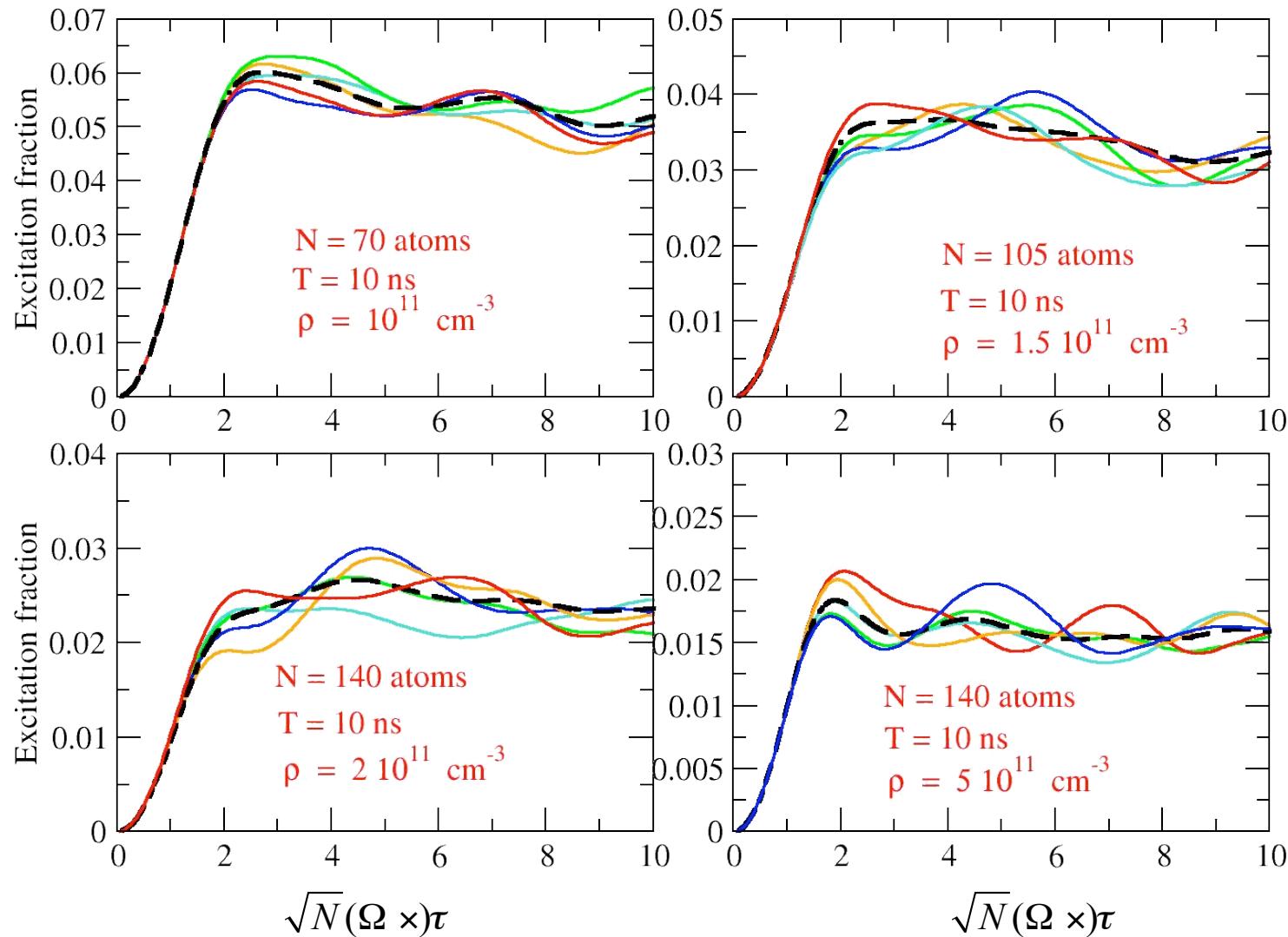
$$\tau = t/\sigma \quad , \quad \omega = \Omega\sigma \quad , \quad k_{ij} = \kappa_{ij}\sigma \quad , \quad \delta = \Delta\sigma$$

$$\frac{d\hat{\sigma}_{ee}^i}{d\tau} = i\frac{\omega}{2} [g(\tau)\hat{\sigma}_{eg}^i - g^*(\tau)\hat{\sigma}_{ge}^i]$$

$$\frac{d\hat{\sigma}_{eg}^i}{d\tau} = i\frac{\omega}{2}g^*(\tau) [2\hat{\sigma}_{ee}^i - 1] + i\sum_{j \neq i} k_{ij}\hat{\sigma}_{eg}^i\hat{\sigma}_{ee}^j$$

- where $g(\tau) = f(\tau)e^{i\delta\tau}$

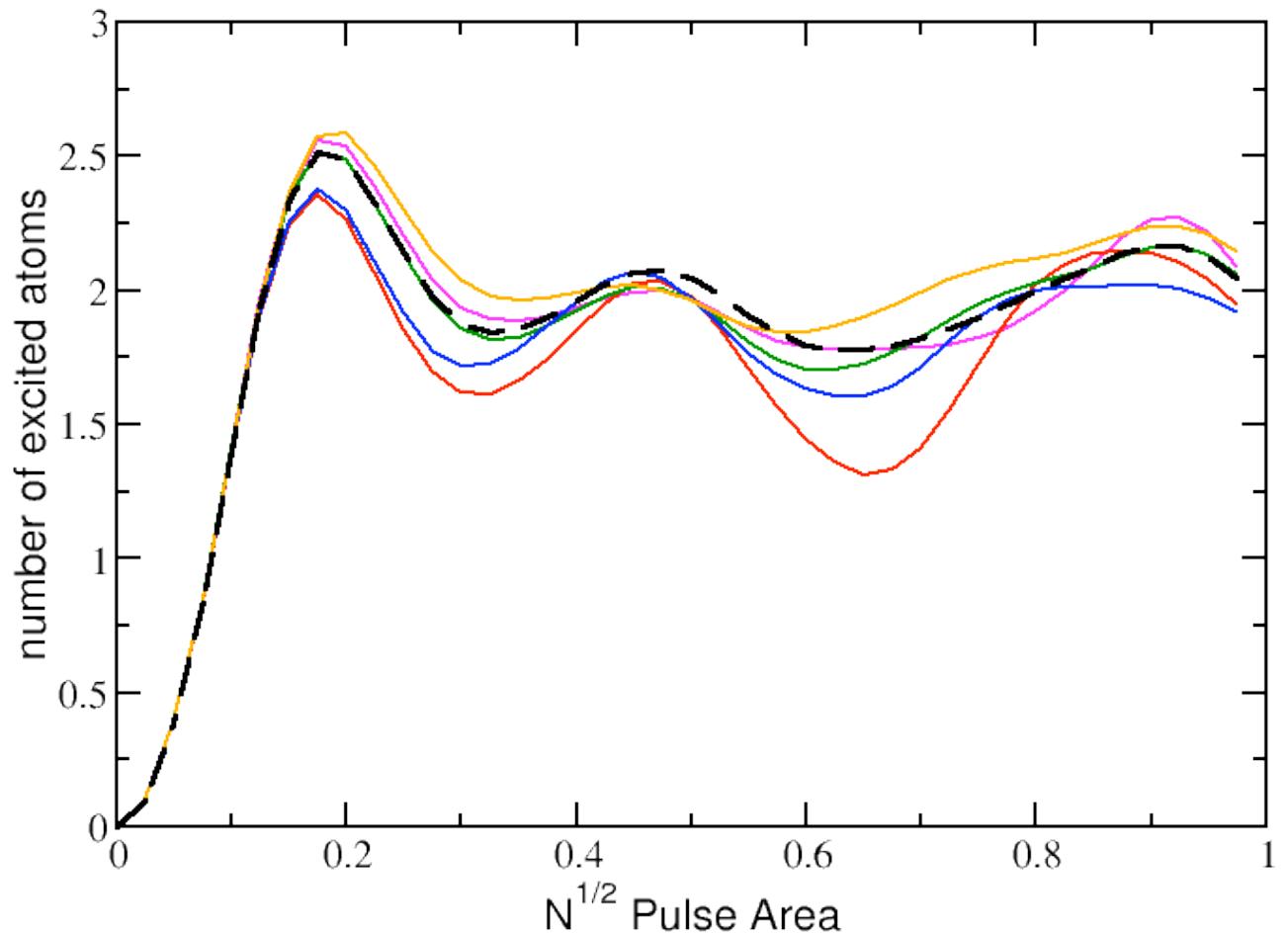
Time dependence



Stronger interactions

- Time-dependent with $n=90$

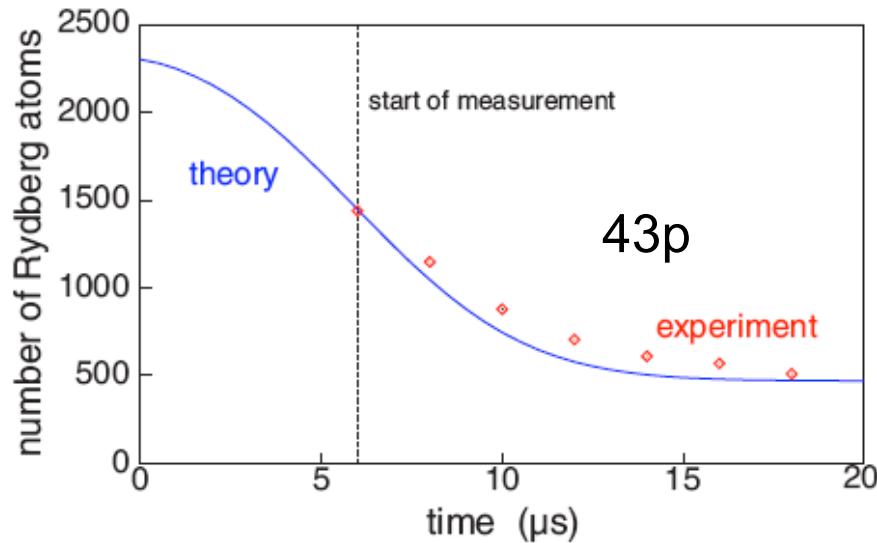
- 70 atoms
 - $\rho = 10^{11} \text{ cm}^{-3}$
 - $\tau = 10 \text{ ns}$
 - Square pulse
 - $V \sim (8 \mu\text{m})^3$



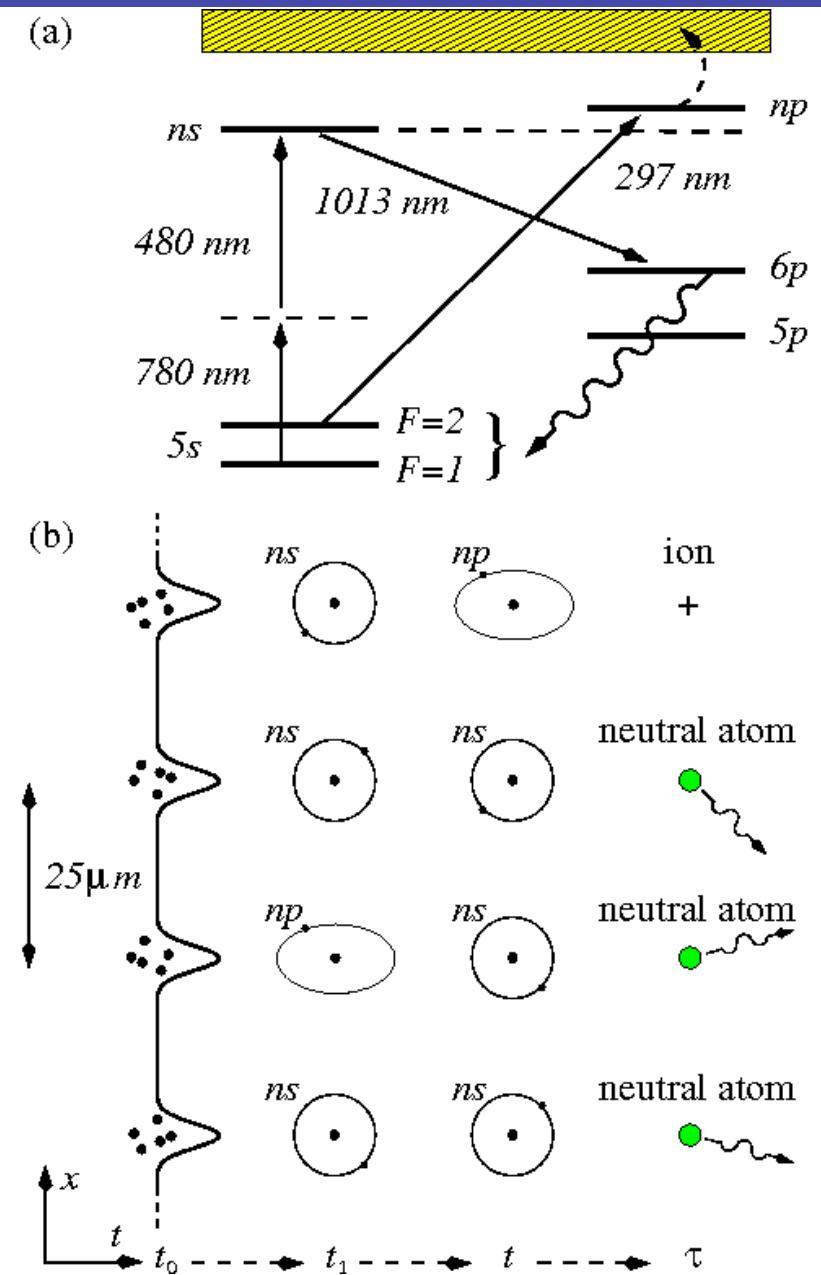
- Fewer excitations (~ 2)

Other studies

- Quantum random walk
 - Diffusion of excitation
 - Prepare using blockade
 - Freiburg and Dresden
- Superradiance

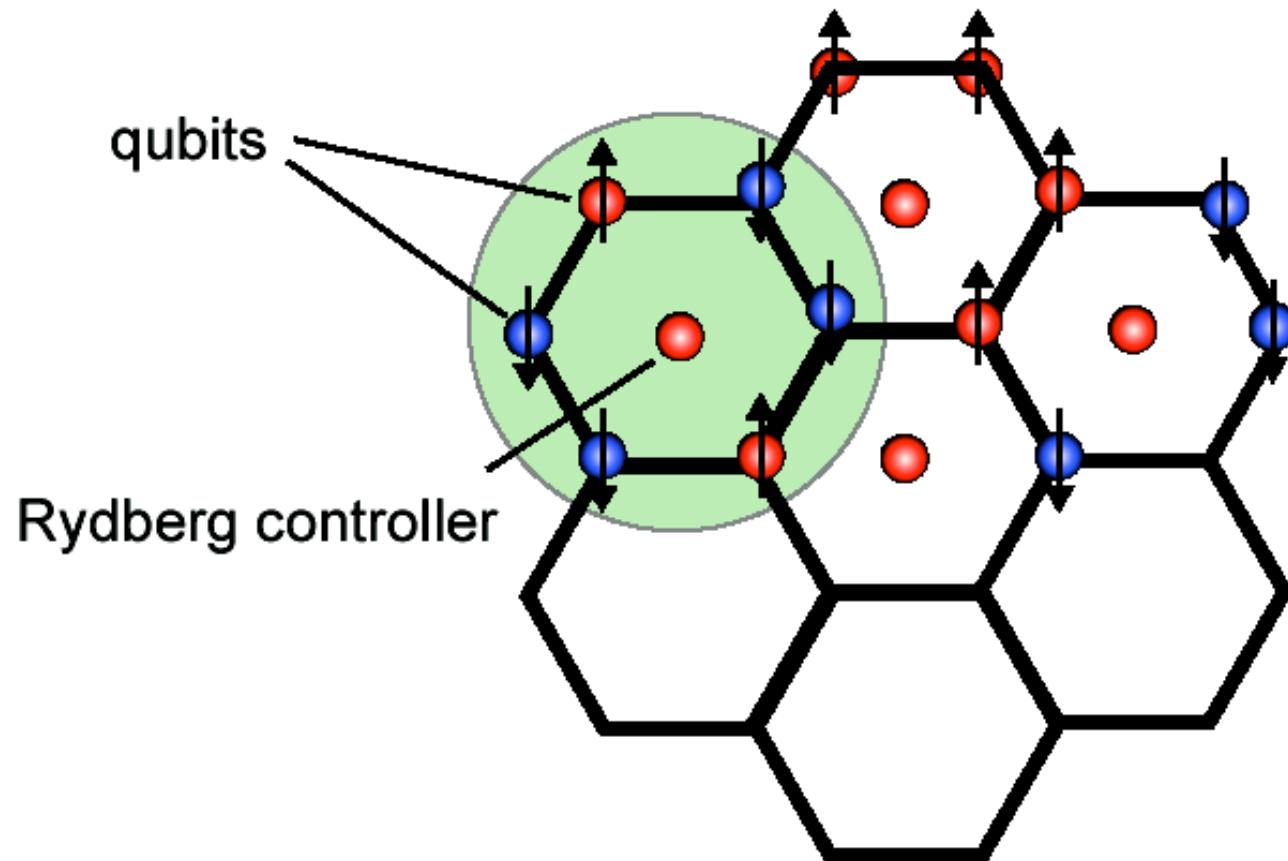


T. Wang et al., PRA 75, 033802 (2007).



Other applications

- Exotic many-body spin systems
 - Kitaev toric code

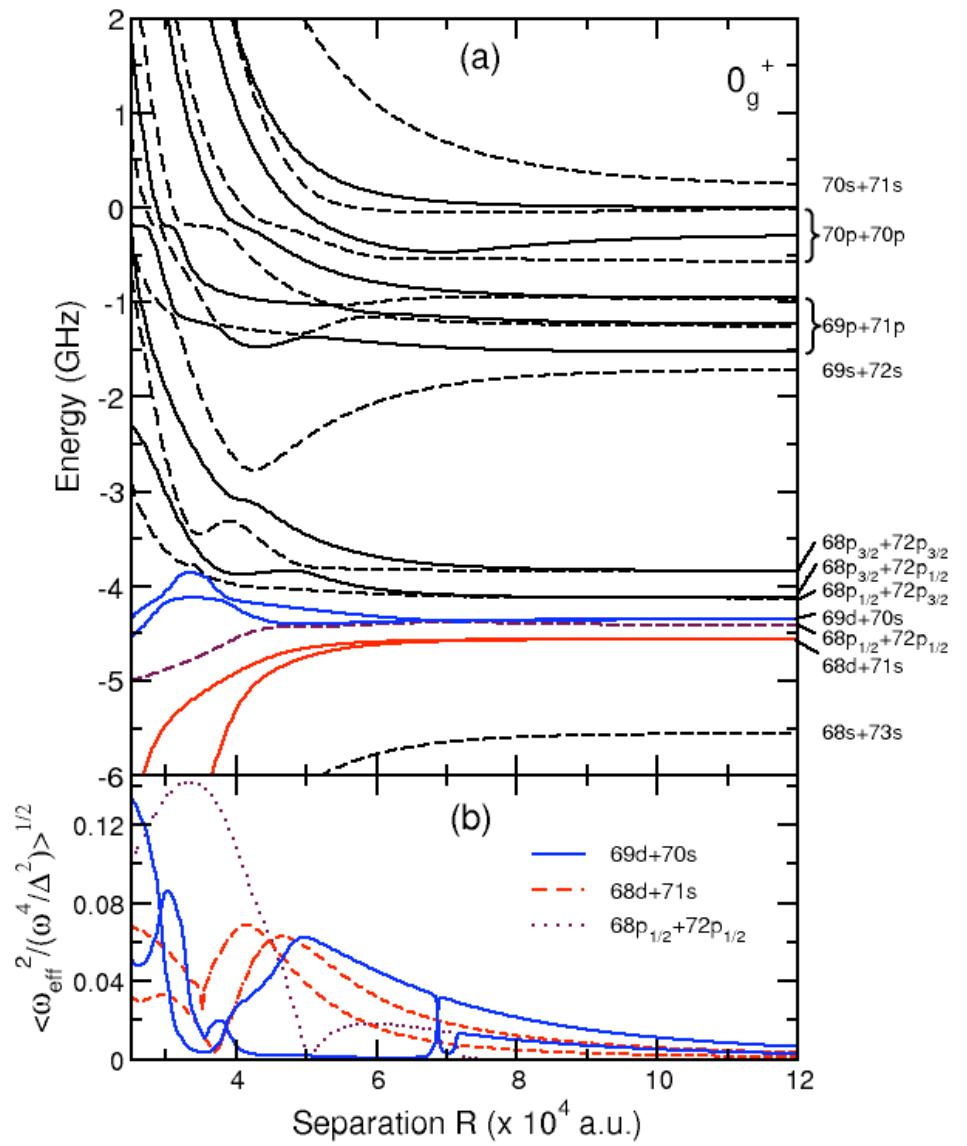
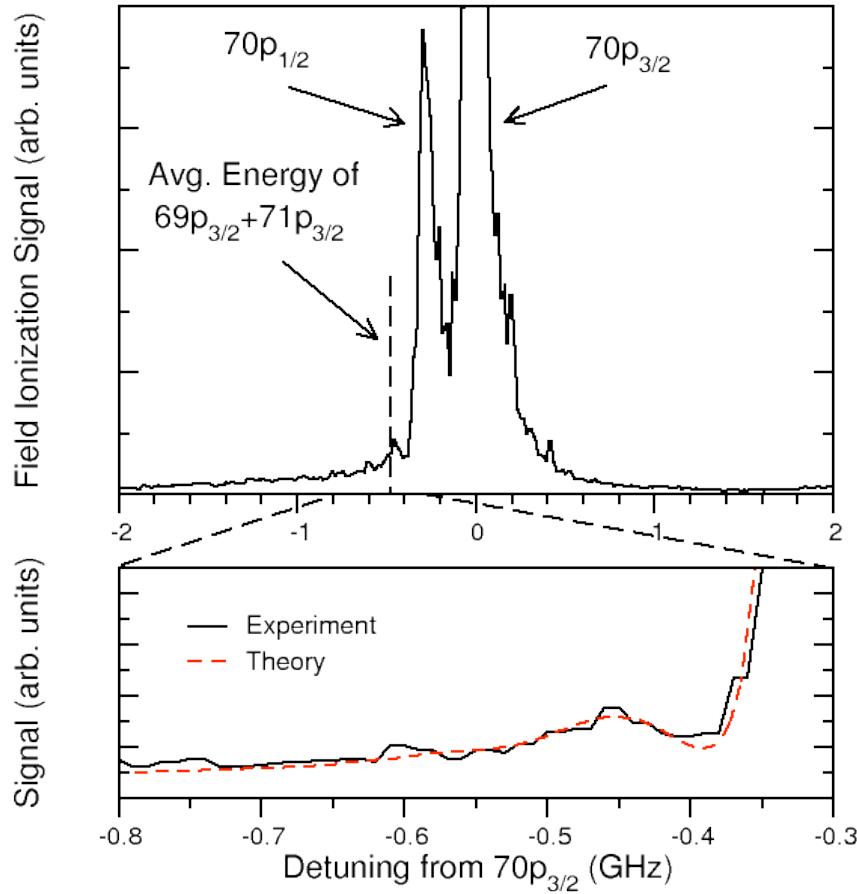


P. Zoller, talk at NSF sponsored workshop (April 2009).

PA in Rydberg gases

- Molecular resonance
 - Curve mixing

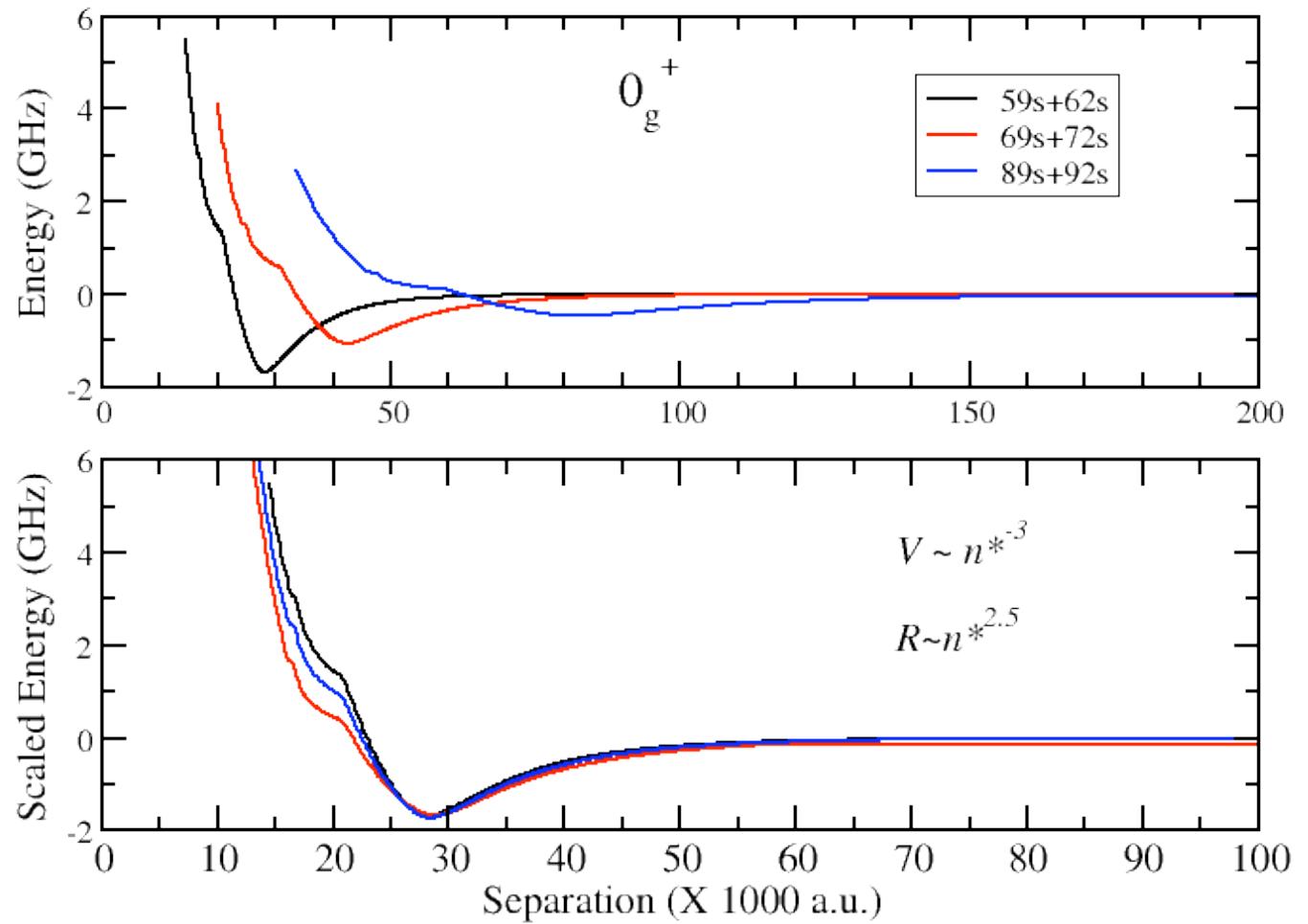
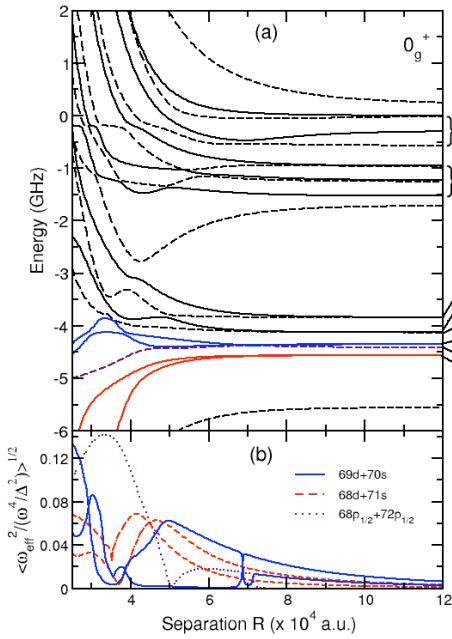
S.M Farooqi *et al.*, PRL **91**, 183002 (2003).
J. Stanojevic *et al.*, EPJD **40**, 3 (2006).



Potential wells

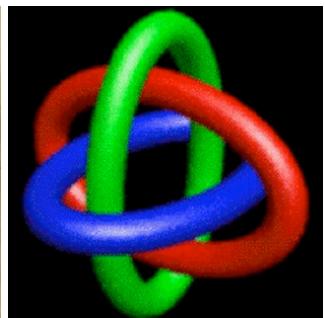
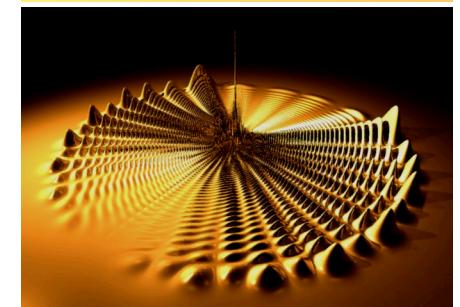
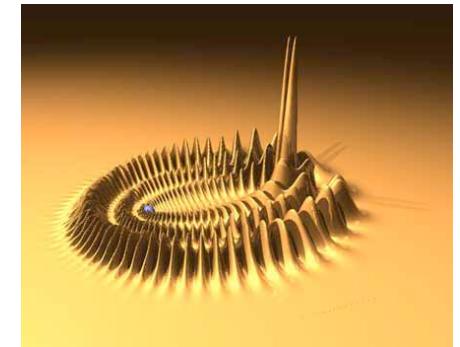
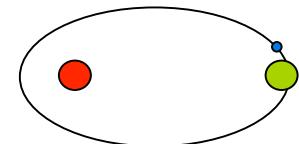
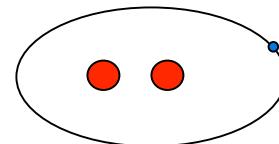
- s+s' & p+p' mixing \Rightarrow wells at shorter separation
 - “macrodimers” (ex., $n=70 \Rightarrow R_e = 103\,000$ a.u.)

- Scaling
 - $R_e \sim n^{*2.5}$
 - $D_e \sim n^{*-3}$



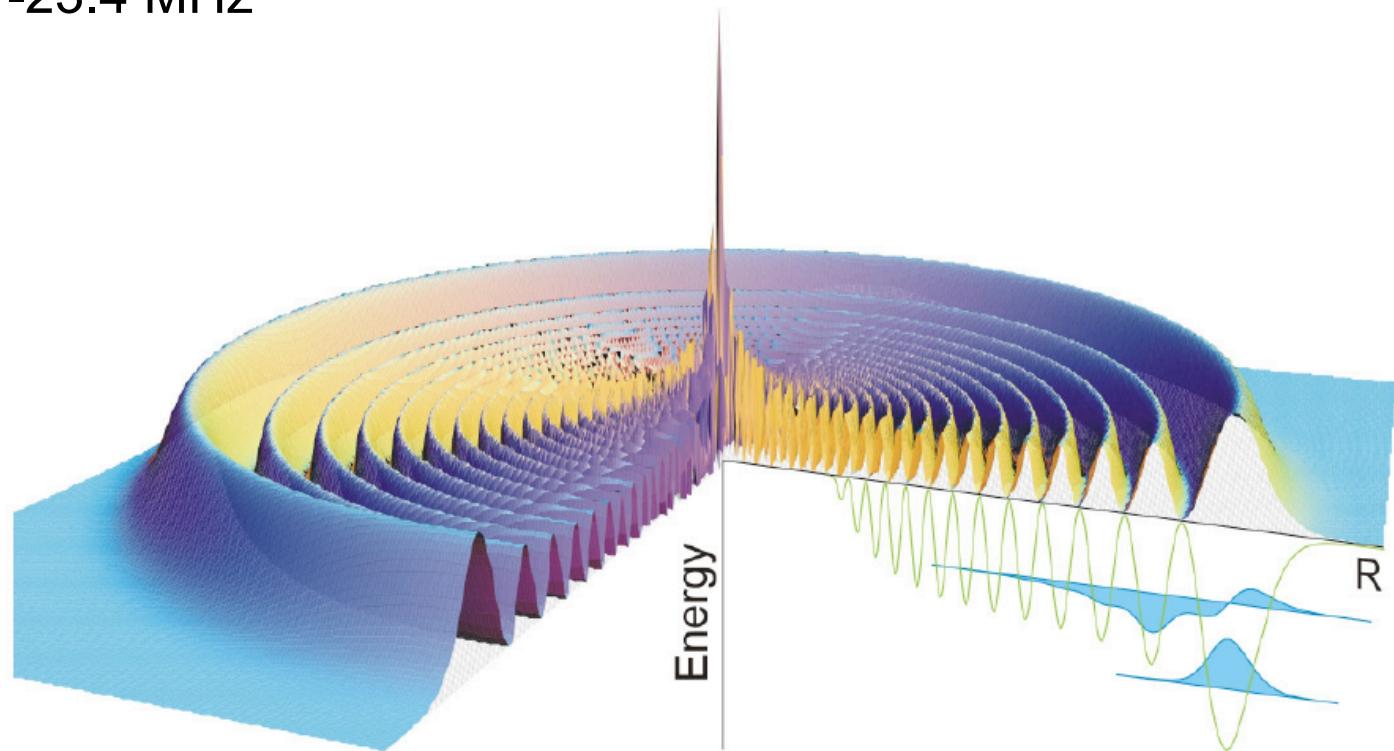
Application: Rydberg Molecules

- “Common” case
 - Tight molecular ion core
 - Loosely bound electron
- Interested in excited molecules with *large internuclear separation R*
- *Giant* Helium dimers produced by $\text{He}(2^3\text{S}\uparrow) + \text{He}(2^3\text{P}\uparrow)$
 - $R \sim 150 - 1150 \text{ } a_0$ and binding energy 1-2 GHz
[Leonard *et al.*, Phys. Rev. Lett. **91**, 073203 (2003)]
- *Trilobite* or *butterfly* states (Greene *et al.*)
 - One atom excited and one in ground state
 - Electron scatters from neutral ground atom
 - ↳ Binding energies $\sim 2\text{GHz}$ at $n=70$
 - ↳ Typical R_e : $500 \text{ } a_0$
- Borromean states (J.M. Rost)



Recent measurements

- Density function for 5s-35s
 - Bound levels observed
 - ▶ $R \sim 1900$ a.u.
 - ▶ $v=0$ at -23.4 MHz



T. Pfau's group, in Nature (2009).

Quick break

- To refresh yourself

